

End Semester Examination, 2021**Semester - III****Physics****PAPER - CC5T***Full Marks : 40**Time : 2 Hours***Gr - A****1. Answer any five of the following :-**

- a) What do you mean by ordinary and singular points in relation to linear differential equations? 2
- b) Write down the applications of Fourier series. 2
- c) Write down the Legendre differential equation with index 1. What are the ordinary and singular points of this equation? 2
- d) What are the mathematical forms of Fourier series for even and odd functions? 2
- e) Give the distribution law of random errors occurred in an experiment. What is the significance of the standard deviation? 1+1
- f) What is Parseval's formula? What is its importance? 1+1
- g) Write down Fuch's theorem? 2
- h) Find the value of x given by 2

$$x = \frac{28.21 \times 2.5 \times 31.4}{315 \times 22.7 \times 1.513}$$

(Turn Over)

Gr - B**Answer any four of the following :-**

2. Compute the relative error in determining acceleration due to gravity from the simple pendulum formula $T = 2\pi\sqrt{\frac{l}{g}}$ for $l = 1\text{m}$ and $T = 2\text{s}$. 5

3. Prove the generating function formula for $P_n(x)$

$$\sum_{n \geq 0} h^n P_n(x) = (1 - 2xh + h^2)^{-1/2}$$

Hence prove $P_n(1) = 1$. 4+1

4. Use the method of Frobenius to find one solution near $x = 0$ of $x^2 y'' + (x^2 + 2x)y' - 2y = 0$. 5

5. Prove that $2\frac{1}{2} + 2\frac{1}{2}$

a) $J_{\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \sin x$

b) $J_{-\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x$

6. If $f(x) = \left(\frac{\pi - x}{2}\right)^2$ in the range of 0 to 2π ,

show that $f(x) = \frac{\pi^2}{12} + \sum_{n=1}^{\infty} \frac{\cos nx}{n^2}$ 5

7. Evaluate $\beta\left(\frac{7}{2}, -\frac{1}{2}\right)$ 5

Gr - C

Answer any one of the following :-

8. Obtain the solution of Laplace's equation for azimuthal symmetry in spherical co-ordinates. 10
- 9.a) Find the complex form of the fourier series

$$f(x) = e^{-x} \quad \text{for } -1 \leq x \leq 1$$

- b) Evaluate $\int_0^{\infty} \sqrt{x} e^{-3\sqrt{x}} dx$ in terms of gamma function.
- c) Show that

$$\beta(p, q) = \int_0^1 \frac{x^{p-1} + x^{q-1}}{(1+x)^{p+q}} dx \quad 3+2+5$$